

# Robustness and Security of Wavelet-Based Watermarking Algorithms

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Several wavelet-based watermarking schemes and their robustness to wavelet compression attacks are discussed. Following an idea by Fridrich [3] and experiments by Kundur [8], we propose to use a parametrization of wavelet filter coefficients to bring the concept of a key-dependent transform to the wavelet domain. We demonstrate that the new technique can be easily integrated in existing watermarking algorithms to improve security.

# Model of the Watermarking Process

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1. generation of a watermark  $W$  (a binary or pseudo-random sequence)
2. embedding the watermark in a host image  $I$ 
  - (a) transform image to a domain suitable for watermarking
  - (b) modify significant coefficients to embed watermark
  - (c) inverse transformation
3. circulation of the watermarked image, possible friendly (e.g. image processing, compression) and unfriendly attacks
4. extraction of the watermark  $W^*$  (blind or with utilization of the original image)
5. normalized watermark correlation

$$\delta = \frac{W^* \cdot W}{\|W^*\| \cdot \|W\|}$$

# Watermarking in the Wavelet Domain

Xia [14] identified several advantages of watermarking in the wavelet domain:

- multiresolution characteristics, hierarchical
- superior modelling of the human visual system (HVS)
- locality
- computational efficiency

Charrier [1] outlines new requirements for the wavelet-based JPEG2000 compression standard:

- coding performance
- progressive transmission, ROI coding, scalability
- security, see <http://eurostill.epfl.ch/~ebrahimi/JPEG2000.htm>

# Kim's Algorithm

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Kim [6] uses level-adaptive thresholding to embed a Gaussian distributed pseudo-random sequence in significant coefficients, similar to Cox [2]

PSNR 38.57



# Wang's Algorithm

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Wang [12] based on MTWC coder [11], similar to Kim

PSNR 33.28

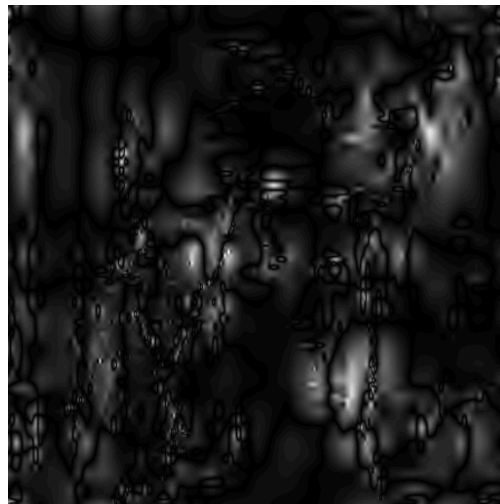
LL $T_4$	$LH_2$ $T_4$	$LH_1$ $T_1$
$HL_2$ $T_6$	$HH_2$ $T_5$	
$HL_1$ $T_3$		$HH_1$ $T_2$

$T_s$  ... initial subband threshold  
approximation subband (LL) not used

$$T_s = \beta_s * \max_s(f_s(m, n))/2$$

$\beta_s$  ... weighting factor for subband  $s$

$\max_s(f_s(m, n))$  ... max. coefficient in subband  $s$



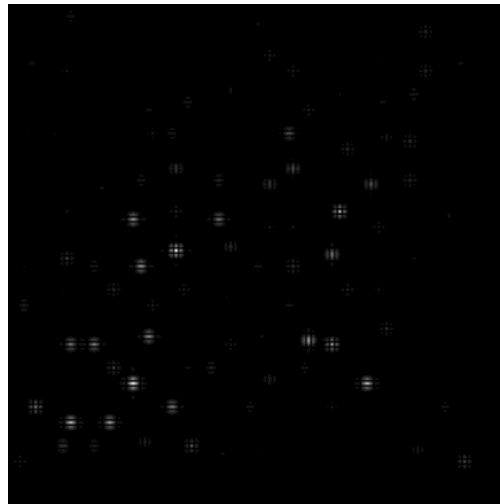
# Kundur's Algorithm

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Kundur [7] is quantizing the median of  $(LH_l, HL_l, HH_l)$  coefficient triples to encode a bit,  $l$  is the decomposition level

locations are pseudo-randomly selected - security?

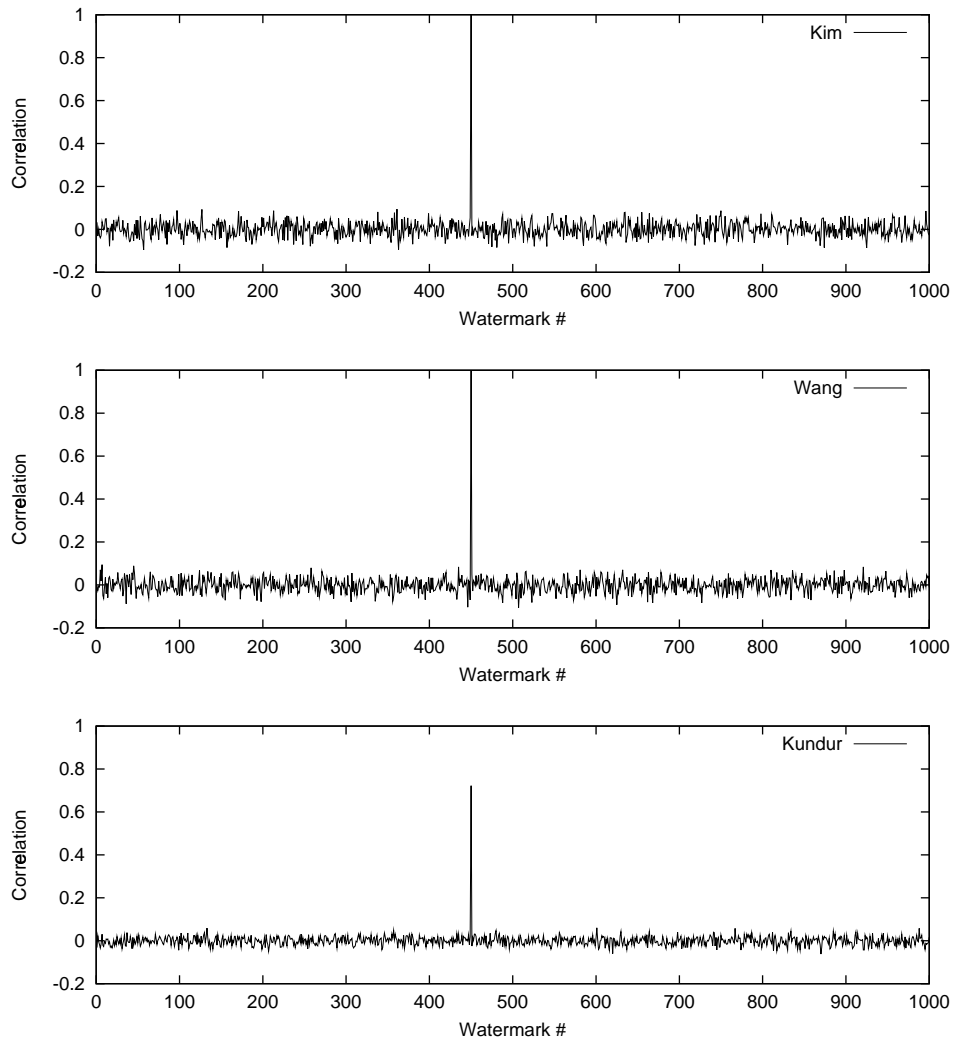
PSNR 52.37



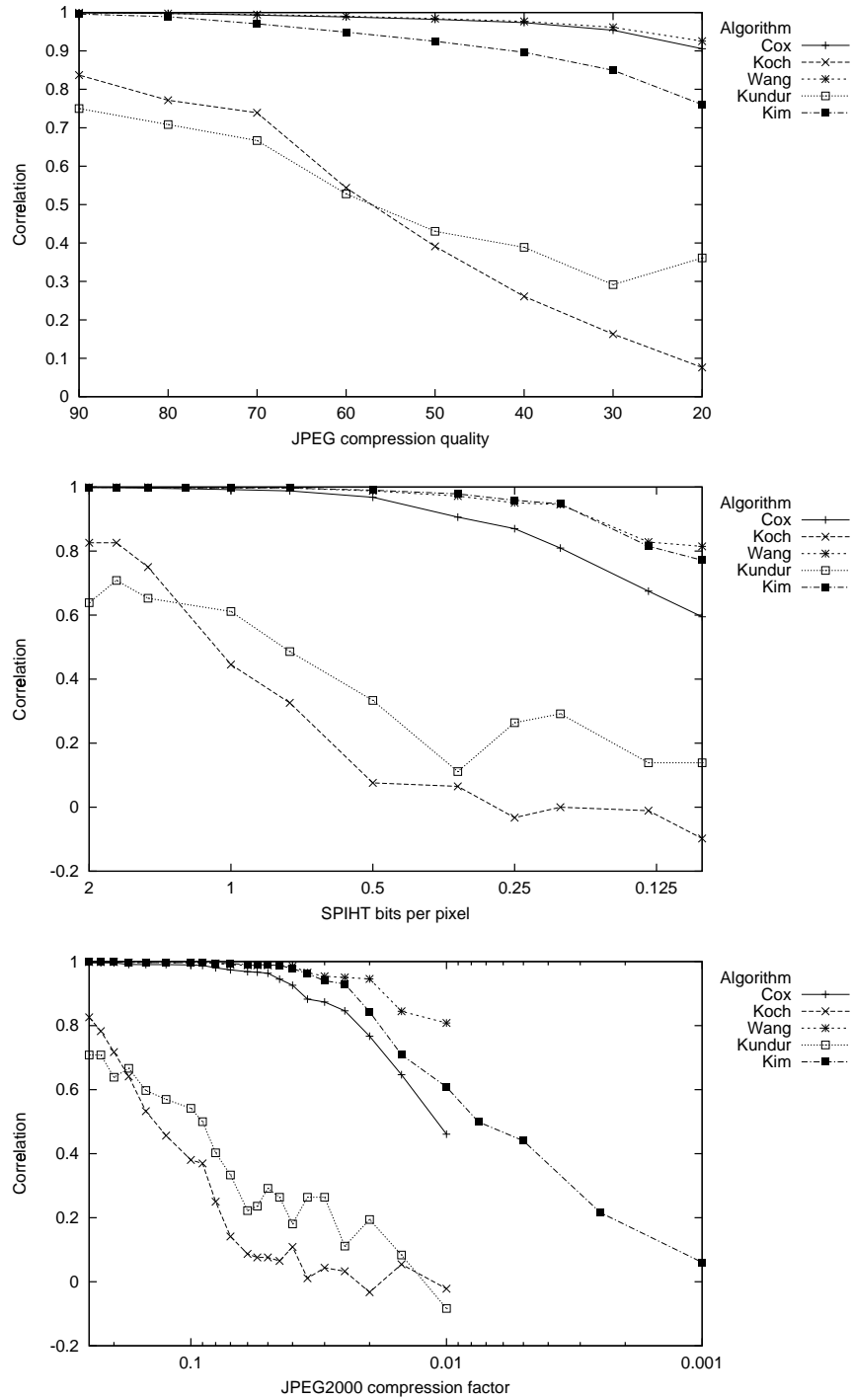
# Detection of the Watermark: Confidence?

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embedded a watermark #450 and trying to detect similar random watermarks #1 to #1000



# Robustness Results





# Security Concerns

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- watermark might be estimated in smooth areas (Fridrich)
- altering coefficients at known or guessed locations (blind algorithms)
- thwarting threshold calculation of blind adaptive schemes (Wang)
- public watermark detector (e.g. for DVD) possible? attacks by Kalker [5]

## Key-dependent basis functions

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an idea by Fridrich [3] to improve security and versatility, embedding a pseudo-random sequence  $w_i$  of length  $N$

1. generate  $N$  random (key-dependent) orthogonal patterns  $P_i$  (Gram-Schmidt), smoothness (low frequency) required for robustness and imperceptability
2. calculate projections  $c_i$  of the host image  $I$  onto the patterns  $P_i$

$$c_i = \langle P_i, I \rangle$$

3. modify the projections to embed the watermark  $w_i$

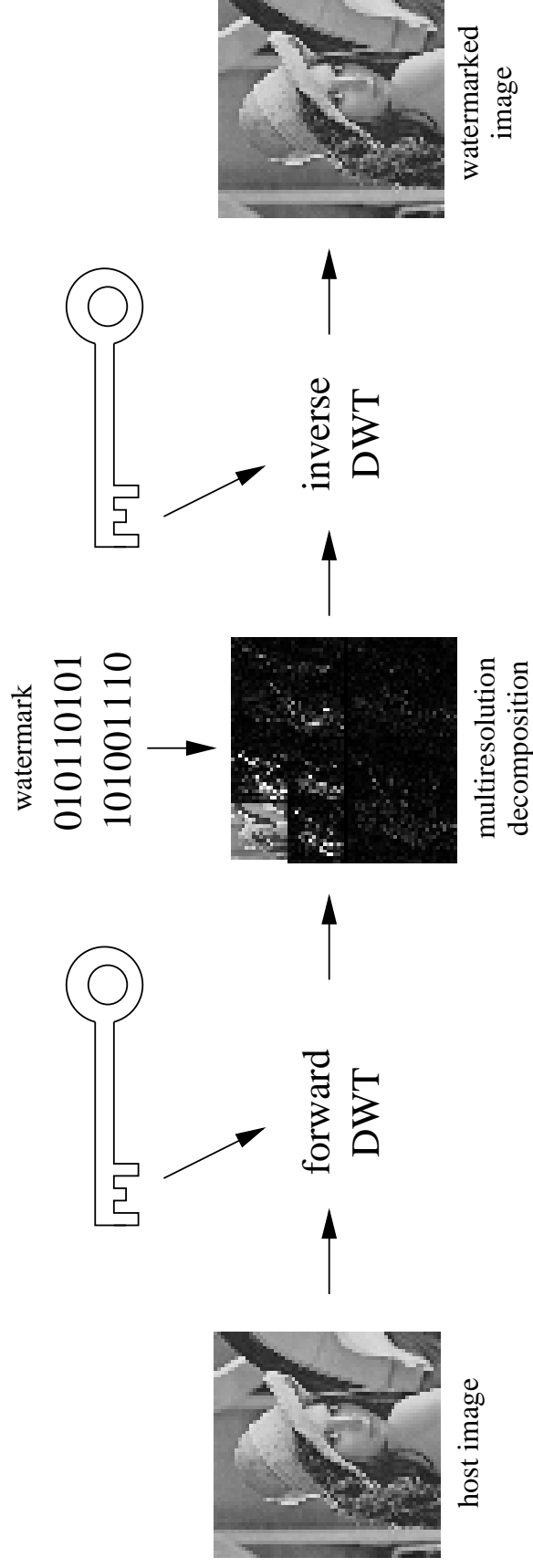
$$I' = I + \alpha \sum_{i=1}^{N-1} w_i c_i P_i$$

high computational complexity and storage requirements

# Key-dependent Wavelet Filters

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wavelet transform domain accessible only with secret parameters used for filter coefficient construction



# Construction of Wavelet Filters by Parametrization

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readily available for orthogonal and bi-orthogonal filter types, e.g. Pollen [9], Zou [15], Resnikoff [10]

Pollen's parametrization for constructing 6-tap orthogonal filter coefficients:

$$a_{-2} = ((1 + \cos \alpha + \sin \alpha) * (1 - \cos \beta - \sin \beta) + 2 * \sin \beta * \cos \alpha) / 4$$

$$a_{-1} = ((1 - \cos \alpha + \sin \alpha) * (1 + \cos \beta - \sin \beta) - 2 * \sin \beta * \cos \alpha) / 4$$

$$a_0 = (1 + \cos(\alpha - \beta) + \sin(\alpha - \beta)) / 2$$

$$a_1 = (1 + \cos(\alpha - \beta) - \sin(\alpha - \beta)) / 2$$

$$a_2 = 1 - a_{-2} - a_0$$

$$a_3 = 1 - a_{-1} - a_1$$

two parameters  $-\pi \leq \alpha, \beta < \pi$  can be kept secret

# Application to Watermarking

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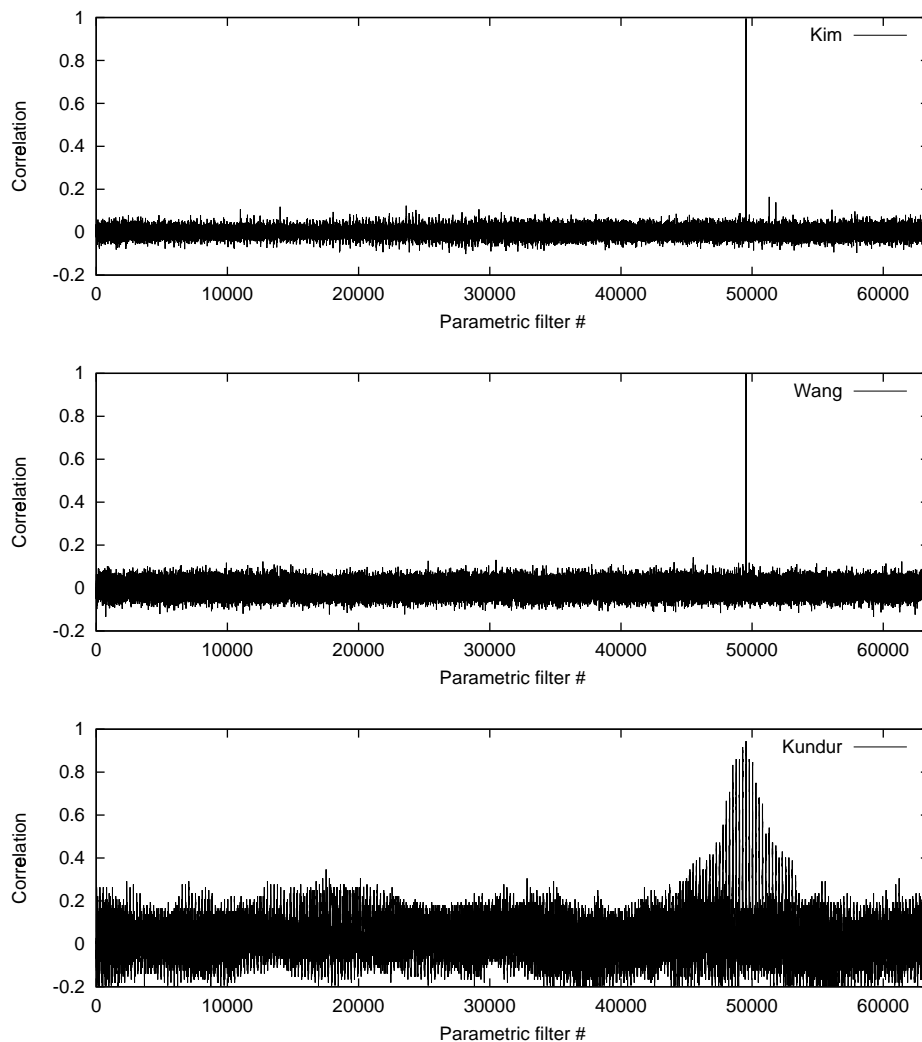
keeping  $\alpha$  and  $\beta$  secret to construct secret wavelet filters

secret transform domain? keyspace?

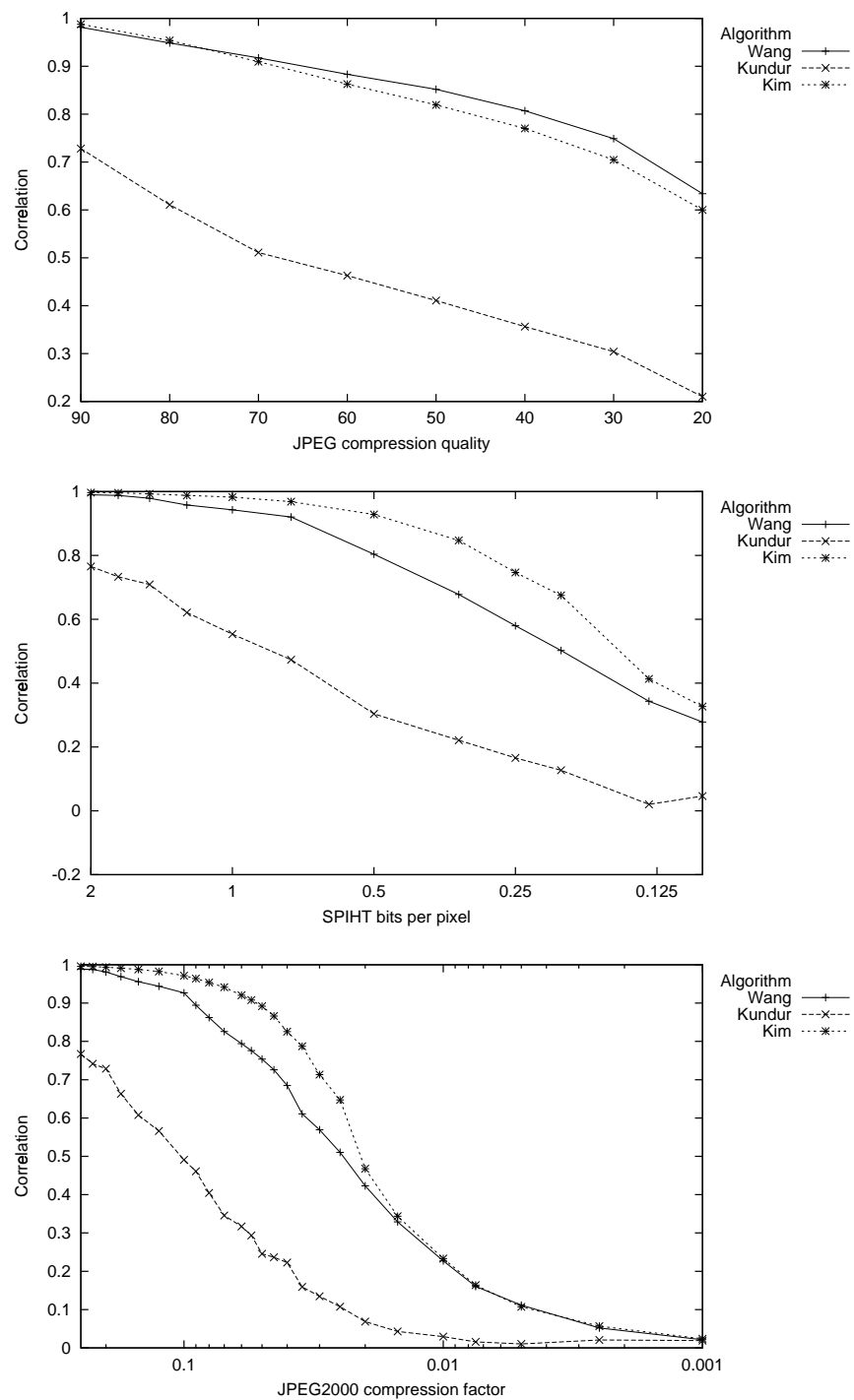
- ✓ no additional computational cost
- ✓ coefficient skipping not necessary for security reasons, more watermark locations for blind schemes
- ✓ security framework for existing watermarking algorithms, only have to adapt thresholds
- ✓ possibility to chose filters in an image-adaptive way

# Detection of the Secret Watermark

embedded a watermark using parametric filter #49560 and detecting the same watermark by trying filter parametrizations #1 to #63504



# Robustness of the Secret Watermark



# Matching watermarking and compression domain?

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dispute by Kundur [8] and Wolfgang [13]: does matching the watermarking and compression domain result in better or worse robustness?

requirements for compression filter and watermarking filter different, Hsu [4]

evaluating different transforms, different wavelet filters

few analysis of unfriendly attacks (exploiting knowledge of the algorithm) so far

security analysis require open algorithms



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