

Blind DT-CWT Domain Additive Spread-Spectrum Watermark Detection

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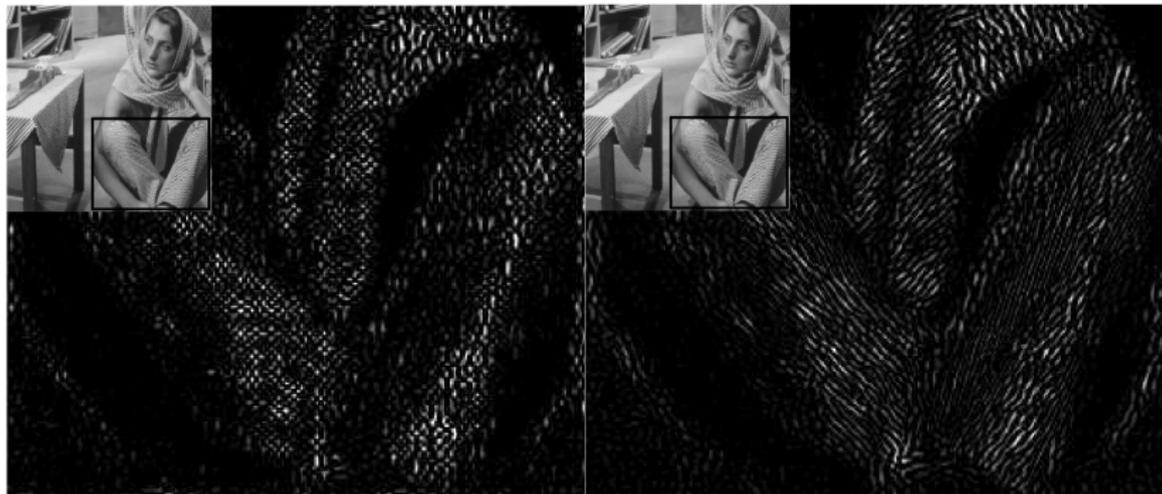
Overview

- ▶ Motivation for DT-CWT watermarking
- ▶ Host signal model for detection
- ▶ Performance evaluation
 - ▶ Perceptual quality assessment
 - ▶ Detection performance / Robustness against compression attack
- ▶ Conclusion

Motivation for DT-CWT Watermarking

Advantages over DWT

- ▶ Better orientational selectivity ($\pm 15^\circ, \pm 45^\circ, \pm 75^\circ$ instead of 3 DWT subbands)
- ▶ Approximately shift invariant.



Previous work

Previous work uses Gaussian host signal model; natural image DCT- and DWT coefficients significantly differ from Gaussian [Hernández et al., 2000]

- ▶ [Wang et al., 2007]: 3D CWT for video watermarking
- ▶ [Coria et al., 2008]: coarse detail coefficient for video watermarking
- ▶ [Woo et al., 2006]: DT-CWT on top of log-polar mapping for geometric invariance.
- ▶ [Tang and Chen, 2009]: motion estimation in the DT-CWT domain for energy-adaptive watermarking
- ▶ non-blind and visible watermarking [Mabtoul et al., 2007, Zhuang and Jiang, 2006]

Host signal model for detection

Propose to model the concatenated real and imaginary DT-CWT coefficients at scale ≥ 2 by a Generalized Gaussian Distribution (GGD).

	Orientation					
Scale	15°	45°	75°	-75°	-45°	-15°
1	6	6	6	6	6	6
2	0	0	0	1	0	0
3	1	0	0	1	0	0

Number of rejects on 6 test images for Kolmogorov-Smirnow test at 1% significance level

Comparing detectors: LC, LRT-GGD, Rao-GGD

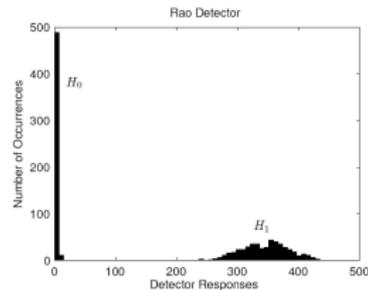
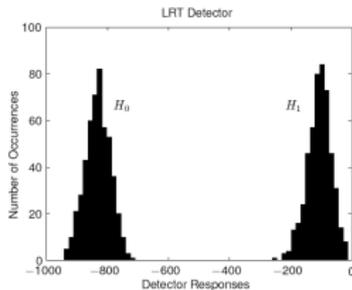
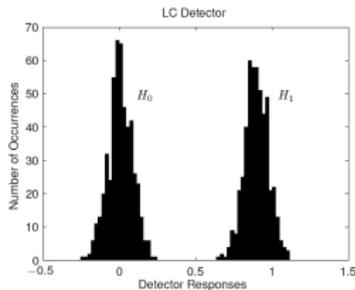
▶ Linear correlation (LC): $\rho_{LC} = \frac{1}{N} \sum_{i=1}^N y_i w_i$

▶ Likelihood-ratio test conditioned on GGD [Hernández et al., 2000]:

$$\rho_{LRT-GGD} = \sum_{i=1}^N \frac{1}{\alpha^\beta} \left(|y_i|^\beta - |y_i - g w_i|^\beta \right)$$

▶ Rao test conditioned on GGD [Nikolaidis and Pitas, 2003]:

$$\rho_{Rao-GGD} = \frac{\left[\sum_{i=1}^N w_i \operatorname{sgn}(y_i) |y_i|^{\beta-1} \right]^2}{\frac{1}{N} \sum_{i=1}^N w_i^2 \left(\sum_{i=1}^N |y_i|^{2\beta-2} \right)}$$



Detection threshold determination

- ▶ Theoretical threshold for LRT-GGD not applicable
 - ▶ need to estimate detection statistic parameters (μ, σ) under H_0
 - ▶ DT-CWT is a redundant transform; watermark embedded in the null-space is lost [Loo, 2002]
 - ▶ can still experimentally compute detection statistic parameters (cumbersome)
- ▶ No problem with Rao-GGD detector
 - ▶ χ^2 distribution, no parameters to estimate

GGD parameter estimation

- ▶ E.g. using Maximum-Likelihood Estimation (MLE) to estimate

$$\beta_0 = 1 + \frac{\psi(1/\hat{\beta})}{\hat{\beta}} - \frac{\sum_{i=1}^N |x_i|^{\hat{\beta}} \log |x_i|}{\sum_{i=1}^N |x_i|^{\hat{\beta}}} + \frac{\log\left(\frac{\hat{\beta}}{N} \sum_{i=1}^N |x_i|^{\hat{\beta}}\right)}{\hat{\beta}}$$

- ▶ Or using fast approximation (not discussed here)
- ▶ Or using fixed parameter: $\beta = 0.8$ or $\beta = 1.0$
- ▶ Note: MLE does not guarantee optimal detection, especially for Rao-GGD detector

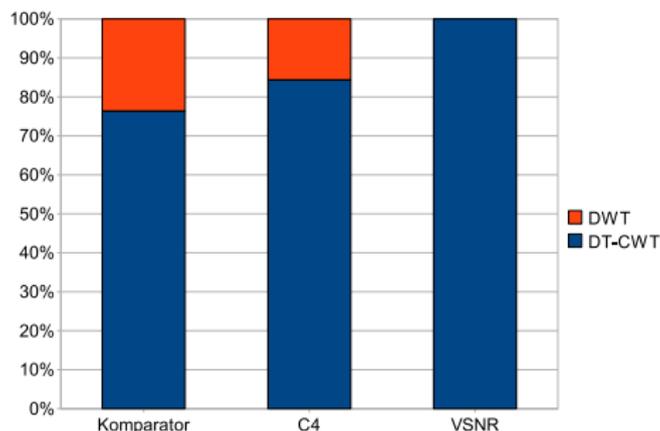
Perceptual quality assessment (1)

- ▶ Employ wPSNR/PQS [Miyahara, 1998], Komparator [Barba and Callet, 2003], C4 [Carnec et al., 2008] and VSNR [Chandler and Hemami, 2007] perceptual metrics
- ▶ Embedding with 36 dB PSNR in DWT and DT-CWT detail subband coefficients
- ▶ Simple perceptual shaping of watermark (proportional to coefficient magnitude)

Image	wPSNR/PQS		Komparator		C4		VSNR	
	DWT	DT-CWT	DWT	DT-CWT	DWT	DT-CWT	DWT	DT-CWT
Lena	45.88	46.49	992.28	799.57	0.939	0.950	23.48	26.53
Barbara	46.81	47.26	1045.24	400.61	0.954	0.957	24.63	27.78
Fabric	46.19	46.90	198.86	320.72	0.966	0.965	30.88	34.67
Bridge	45.96	46.49	556.719	506.745	0.941	0.960	26.21	29.43
Dromedary	45.95	46.52	1059.48	387.69	0.923	0.946	22.78	25.56
Models	45.75	46.29	672.59	444.81	0.957	0.963	28.60	31.90

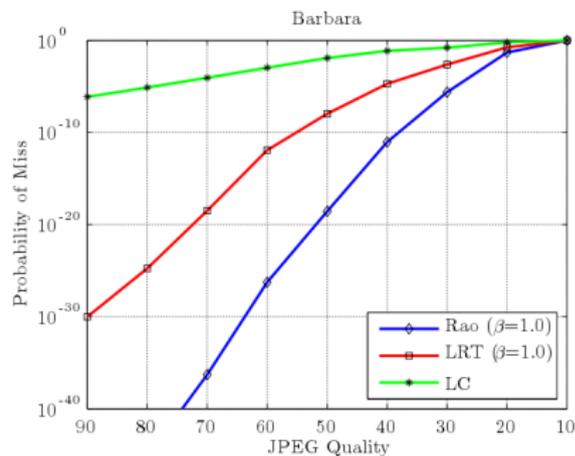
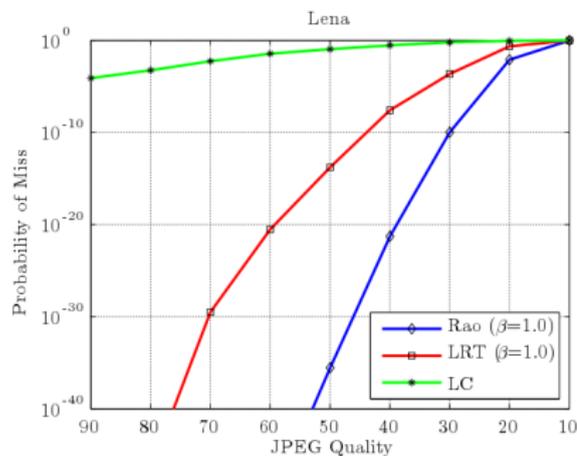
Perceptual quality assessment (2)

- ▶ Experiments with 500 grayscale images, same setup as before
- ▶ Number of images per embedding domain (DT-CWT vs. DWT) that were judged higher quality
 - ▶ Komparator: 382 DT-CWT / 118 DWT
 - ▶ C4: 422 DT-CWT / 78 DWT
 - ▶ VSNR: 500 DT-CWT / 0 DWT



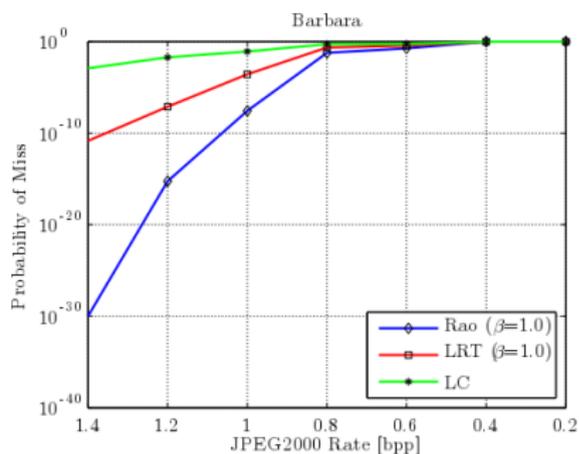
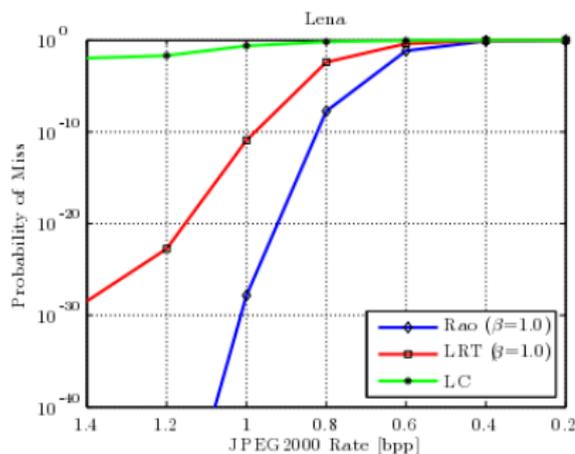
Detection performance under attack: JPEG

- ▶ Experimental evaluation with $N = 1000$ different watermarks embedded with DWR 16 dB
- ▶ Estimate detection statistic under H_0 (other watermark) and H_1 (correct watermark)
- ▶ Plot Probability of Miss P_m for False-Alarm Rate $P_f = 10^{-10}$ after JPEG compression



Detection performance under attack: JPEG2000

- ▶ Experimental evaluation with $N = 1000$ different watermarks embedded with DWR 16 dB
- ▶ Estimate detection statistic under H_0 (other watermark) and H_1 (correct watermark)
- ▶ Plot Probability of Miss P_m for False-Alarm Rate $P_f = 10^{-10}$ after JPEG2000 compression



Conclusion

- ▶ Concatenated real and imaginary DT-CWT detail subband components can be modeled by GGD
- ▶ Performance of linear correlation can be improved (non-Gaussian distribution) by Rao-GGD and LRT-GGD detector
- ▶ MLE of GGD shape parameter does not necessarily lead to best detection performance
- ▶ Objective perceptual assessment indicate higher quality of DT-CWT embedded watermark
- ▶ Source code available at <http://www.wavelab.at/sources>

References



Barba, D. and Callet, P. L. (2003).

A robust quality metric for color image quality assessment.

In *Proceedings of the IEEE International Conference on Image Processing, ICIP '03*, volume 1, pages 437–440, Barcelona, Spain. IEEE.



Carnec, M., Callet, P. L., and Barba, D. (2008).

Objective quality assessment of color images based on a generic perceptual reduced reference.

Signal Processing: Image Communication, 23(4):239–256.



Chandler, D. and Hemami, S. (2007).

VSNR: A wavelet-based visual signal-to-noise ratio for natural images.

IEEE Transactions on Image Processing, 16(9):2284–2298.



Coria, L., Pickering, M., Nasiopoulos, P., and Ward, R. (2008).

A video watermarking scheme based on the dual-tree complex wavelet transform.

IEEE Transactions on Information Forensics and Security, 3(3):466–474.



Hernández, J., Amado, M., and Pérez-González, F. (2000).

DCT-domain watermarking techniques for still images: Detector performance analysis and a new structure.

IEEE Transactions on Image Processing, 9(1):55–68.



Loo, P. (2002).

Digital Watermarking with Complex Wavelets.

PhD thesis, University of Cambridge, United Kingdom.



Mabtoul, S., Hassan, E., Elhaj, I., and Aboutajdine, D. (2007).

Robust color image watermarking based on singular value decomposition and dual tree complex wavelet transform.

In *Proceedings of the 14th IEEE International Conference on Electronics, Circuits and Systems, ICECS '07*, pages 534–537. IEEE.



Miyahara, M. (1998).

Objective picture quality scale (PQS) for image coding.